


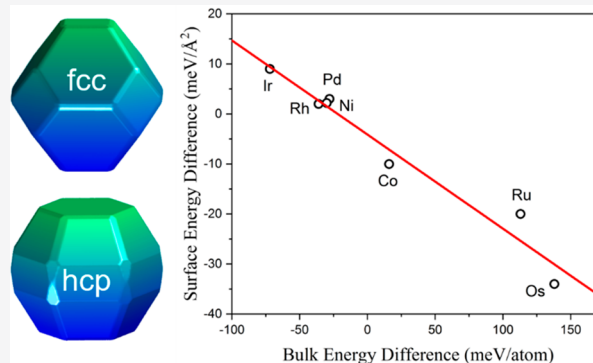
Compensation between Surface Energy and hcp/fcc Phase Energy of Late Transition Metals from First-Principles Calculations

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ABSTRACT: Crystal structures and surface energies of transition metals are of fundamental importance to the activity, selectivity, and stability in heterogeneous catalysis, but the interplay between crystal structures and surface energies as well as its dependence on composition remains elusive. In the present work, we performed comprehensive density functional theory calculations of Co, Ni, Ru, Rh, Pd, Os, and Ir in both hexagonal close-packed (hcp) and face-centered cubic (fcc) phases and considered numerous surfaces to derive the equilibrium morphology and the surface energy. Irrespective of the transition metals considered, the fcc phase exposes mainly {111} and {100} facets, whereas the hcp phase exposes mainly {0001}, {10 $\bar{1}$ 0}, and {10 $\bar{1}$ 1} facets. For Co, Ru, and Os preferring the hcp bulk at ambient conditions, the corresponding surface energies are found higher to be than those in the fcc bulk, whereas for Ni, Rh, Pd, and Ir preferring the fcc bulk phase at ambient conditions, the opposite trend is found. A negative linear relationship of the surface energy difference between the fcc and hcp phases with respect to the corresponding bulk energy difference is established; a phase with a higher bulk energy has a lower surface energy as compensation. The compensation effect on the surface energy and the bulk energy provides a driving force for the size-induced phase transition of the nanoparticles. The results are used to rationalize the available experiments, and the insights revealed might be used to design better catalysts.



INTRODUCTION

Transition metals (TMs) have been widely used to catalyze various chemical reactions in heterogeneous catalysis.^{1,2} Corresponding catalysts with specific size and shape are prepared to expose more coordinate-unsaturated sites and/or unique ensembles (such as BS sites) to optimize the catalytic activity and selectivity.^{3–6} Exploring the sensitivity of active sites with different structural motifs is thus important to design new catalysts.^{7–11} Among others, there has been increasing interest in the effect of crystal structures on heterogeneous catalysis and electrocatalysis.^{12–14} The great impact of crystal phases on catalysis mainly comes from their distinct bulk symmetries, which might result in various structural motifs with highly different reactivity and density.^{15–17} Many experiments reported that for Fischer–Tropsch synthesis (FTS) cobalt with a hexagonal closed-pack (hcp) phase is more active than that with a face-centered cubic (fcc) one.^{18–22} Theoretical calculation found that higher activity of hcp Co came from the exposure of more open surfaces with higher intrinsic activity.²³ However, for ruthenium, the fcc phase was able to expose more active sites and therefore have a higher specific activity than hcp Ru, as confirmed by subsequent FTS experiment.²⁴ Higher activity of fcc Ru than hcp Ru is also found for CO oxidation, hydrogen oxidation

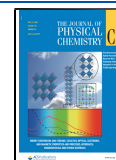
reaction, ammonia–borane, oxygen evolution reaction, hydrogenation reaction, and N₂ activation.^{25–32} Additionally, it is also found that CO methanation and aqueous-phase reforming of glycerol over Ni are crystal structure dependent.^{33,34} Investigations of different crystal phases of transition metals and their phase transition are therefore helpful to rationalize the involved structure–activity relationship of supported nanocatalysts at relevant catalytic reaction conditions.

For bulk TMs at ambient conditions, the favorable crystal phase follows the sequence of hcp–bcc–hcp–fcc, from the left to right side of the periodic table, due to their different electron configurations.³⁵ For catalytic relevant bulk metals at ambient conditions, Co, Ru, and Os prefer the hcp phase, whereas the late transition metals such as Ni, Cu, Rh, Pd, Ag, Ir, Pt, and Au prefer the fcc phase.^{36–42} At elevated temperatures and high pressures, which are applied typically for most catalytic

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reactions, the active phase of the metal catalysts might transit from one phase to another.^{43–45} Since most catalysts are highly dispersed and interact strongly with the substrates underneath,^{46,47} the surface/interface effect would become important.^{48,49} In particular, when decreasing the particle size to nanometers, the contribution of the surface energy to the overall energetics of a nanoparticle increases dramatically and might change the relative stability of nanoparticles with different phases.⁵⁰ However, it is unclear yet how surface energy changes with the crystal phases and the compositions, and what the impact is on the phase transition with respect to the decrease of the particle size.

To shed further light on this, we performed extensive DFT calculations on the surface energies of fcc and hcp TMs including Co, Ni, Ru, Rh, Pd, Os, and Ir. In order to get the overall surface energy, numerous surfaces with different orientations (13 for fcc and 12 for hcp) were considered. The equilibrium morphology of these TMs is derived, and the fcc phase is found to be dominated by {111} and {100} facets, whereas the hcp phase is dominated by {10 $\bar{1}$ 0}, {10 $\bar{1}$ 1}, and {0001} facets, irrespective of the TMs considered. Based on the optimized morphologies, the corresponding overall surface energies are calculated. For Co, Ru, and Os, the corresponding hcp surface energies are found to be higher than those of the fcc phase, whereas for Ni, Rh, Pd, and Ir, the opposite trend is found. A negative linear relationship of the surface energy difference between the fcc and hcp phases with respect to the corresponding bulk energy difference is established. The lower the bulk energy of a crystal phase, the higher the surface energy as compensation. The compensation effect provides a potential driving force for the phase transition for small particles, which might be used to design better catalysts.

METHODOLOGY

All spin-polarized DFT calculations were performed using the Vienna *Ab Initio* Simulation Package (VASP)^{51–53} within the projector augmented wave (PAW) approach.^{54,55} The exchange–correlation effects were modeled using the Perdew–Burke–Ernzerhof (PBE) generalized gradient approximation (GGA) functional,^{56,57} and the plane wave cutoff energy was specified as 400 eV. The energy and maximum force convergence thresholds were set to 10^{−5} eV and 0.01 eV/Å, respectively. The Methfessel–Paxton method was chosen as the smearing algorithm,⁵⁸ and the blocked Davidson iteration scheme was chosen as the electron minimization algorithm.⁵⁹ Γ -centered k -points meshes of 50/a × 50/b × 50/c and 50/a × 50/b × 1 were used for bulk and slab calculations, respectively. We used vacuum thicknesses of 15 Å to separate the interactions between neighboring slabs to ensure convergence.

Surface free energy is the energy cost to create a new surface per unit area by truncating the metal–metal bond through the specific surface. The accurate measurement of surface energies, especially for high-index facets, remains difficult and even unavailable for the metastable phase.⁶⁰ In contrast, DFT provides a systematic method to calculate surface energy.^{61–64} In the present work, the surface energy γ_{hkl} of the TMs facet featuring Miller-index (hkl) can be calculated by taking the energy difference between the total energy of an N -layer slab (E_N) and an equivalent bulk reference amount (NE_B) per surface area, determined by

$$\gamma_{hkl} = \lim_{N \rightarrow \infty} (E_N - NE_B) / 2A \quad (1)$$

A is the surface area of the slab model. We then use the method suggested by Fiorentini and Methfessel to minimize the possible numerical error introduced by a different supercell.⁶⁵ Specifically, for sufficiently large N , varying from 15 to 40, depending on the surface orientation, one can rewrite eq 1 as

$$E_N = 2\gamma_{hkl}A + E_B \times N \quad (2)$$

Obviously, if the total energy of the slab depends linearly on the slab thickness N , the slope and intercept give the bulk energy and surface energy, respectively.

By using the calculated surface energies, the equilibrium morphology of a freestanding particle can be obtained by the Gibbs–Wulff theorem.^{66,67} The Wulff construction can be executed as follows: starting from a center point, a plane that is normal to the $\langle hkl \rangle$ vector (taking fcc as an example) is drawn at the distance of $d_{hkl} = C \times \gamma_{hkl}$ where C is a given constant and γ_{hkl} is the surface energy of unit area normal to the $\langle hkl \rangle$ vector. Once this process is repeated for all the Miller-index planes, the polyhedron that lines inside all the planes gives the equilibrium morphology of the crystal. The Wulff morphologies of various TMs were constructed by VESTA software in the present work.⁶⁸ Given that the transition metals expose different facets i with surface energy γ_i and corresponding surface ratio f_i , the overall surface energy γ is calculated via

$$\gamma = \sum_i f_i \times \gamma_i \quad (3)$$

RESULTS AND DISCUSSION

Bulk Property. We first describe here the calculated bulk properties. For convenience, we classify the TMs considered into two groups based on their favorable bulk structure at ambient conditions: Group I, in which Co, Ru, and Os prefer the hcp phase, and Group II, in which Ni, Rh, Pd, and Ir prefer the fcc phase. Calculated bulk energy differences per atom between the fcc and hcp phases ($\Delta E_B(\text{fcc} - \text{hcp})$) and the corresponding optimized lattice constants are shown in Figure 1 and Table 1, respectively. From Figure 1, it can be found that for the TMs in Group I, the hcp bulk energies are all lower

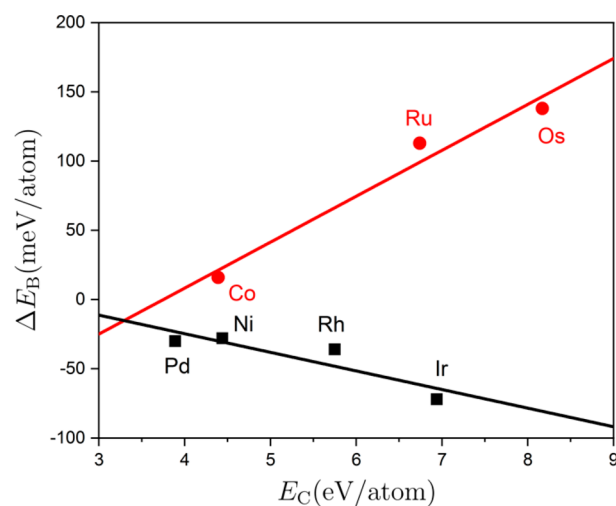


Figure 1. Relationship between crystal phase energy (ΔE_B) and the experimentally measured cohesive energy (E_C) of the seven late transition metals in their most stable bulk phase.

Table 1. Optimized Lattice Constants (a for fcc Phase, a and c for hcp Phase, Å) of Seven Late Transition Metals^a

elements	fcc		hcp				ΔE_B
	a	expt	a	expt	c	expt	
Co	3.520	3.544 ⁶⁹	2.491	2.507 ⁷⁰	4.027	4.070	16
Ru	3.818	3.87 ⁷⁶	2.727	2.706 ⁷¹	4.300	4.282	113
Os	3.855	3.810 ⁷²	2.754	2.735 ⁷²	4.343	4.319	138
Ni	3.520	3.524 ⁷⁷	2.482	2.622 ⁷⁹	4.097	4.321	-28
Rh	3.841	3.804 ⁶⁹	2.729	2.78 ⁸¹	4.408	4.64	-36
Pd	3.949	3.891 ⁷⁸	2.771	2.64 ⁸²	4.653	4.88	-30
Ir	3.877	3.839 ⁷⁸	2.751	–	4.464	–	-72

^aExperimental lattice constants we can obtain so far are also listed. The calculated bulk energy differences between the fcc and hcp phases per atom (ΔE_B , meV/atom) are tabulated in the last column. The lattice constants for the favorable crystal structure of transition metals under ambient conditions are highlighted in bold text.

Table 2. Calculated Surface Energies γ_i of Late Transition Metals with fcc Crystal Structure in Unit of meV/Å², f_i is Corresponding Exposure Surface Ratio (%)^a

fcc	Co		Ru		Os		Ni		Rh		Pd		Ir	
	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i
{100}	153	14	187	6	227	6	136	20	145	17	94.1	19	175	12
{110}	150	10	173	2	207	–	140	–	148	4	99.4	–	176	–
{111}	129	62	148	61	168	65	119	56	125	65	83.3	51	142	56
{210}	162	–	191	–	235	–	148	–	157	–	102	1	188	–
{211}	152	–	175	4	206	1	137	6	146	–	95.1	4	169	–
{221}	146	–	165	6	191	–	134	–	141	6	93.1	10	162	–
{310}	164	–	191	1	231	–	148	–	156	1	101	2	189	–
{311}	156	9	183	9	223	–	142	1	150	8	100	–	179	–
{320}	159	–	188	–	226	–	146	–	155	–	102	–	184	–
{321}	155	–	178	3	211	–	143	–	152	–	99.1	–	178	–
{322}	144	–	166	–	190	15	131	3	140	–	90.8	10	157	18
{331}	151	–	169	8	197	–	136	12	146	–	96.5	–	170	–
{332}	140	4	161	–	183	14	129	1	138	–	90.2	2	154	14
γ	136		159		179		125		134		87.4		150	

^a–, exposure ratio less than 1%; γ is the resultant overall surface energy.

Table 3. Calculated Surface Energies γ_i of Late Transition Metals with hcp Crystal Structure in Unit of meV/Å², f_i is Corresponding Exposure Surface Ratio (%)^a

hcp	Co		Ru		Os		Ni		Rh		Pd		Ir	
	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i	γ_i	f_i
{0001}	131	18	163	15	182	19	115	17	122	17	77.9	18	132	20
{10 $\bar{1}$ 0}	141	24	181	21	213	26	121	23	129	21	84.6	24	142	28
{10 $\bar{1}$ 1}	149	30	180	41	216	40	124	46	130	47	87.2	40	146	47
{10 $\bar{1}$ 2}	156	12	189	13	225	10	135	6	143	4	93.0	9	161	–
{11 $\bar{2}$ 0}	153	7	209	–	256	–	136	1	147	–	95.4	–	174	–
{11 $\bar{2}$ 1}	162	–	204	–	246	–	141	–	149	–	98.0	–	174	–
{11 $\bar{2}$ 2}	161	5	195	5	236	4	137	2	141	7	95.5	4	160	4
{20 $\bar{2}$ 1}	149	3	186	1	222	–	126	1	134	–	89.9	–	153	–
{21 $\bar{3}$ 0}	154	–	205	–	246	–	134	2	143	1	93.8	2	164	–
{21 $\bar{3}$ 1}	160	–	202	2	241	2	139	–	146	–	97.3	–	166	–
{21 $\bar{3}$ 2}	161	1	199	1	241	–	138	1	146	–	97.4	–	166	–
{22 $\bar{4}$ 1}	159	–	207	–	256	–	140	–	144	4	96.2	2	168	–
γ	146		179		213		122		132		85.2		141	

^a– for exposure ratio less than 1%; γ is the resultant overall surface energy.

than the fcc bulk energies, but the opposite trend is found for the TMs in Group II. This means that for the TMs in Groups I and II, hcp phase and fcc phase is the preferential phase structure, respectively, in perfect agreement with experiments. Specifically, corresponding ΔE_B values are 16, 113, and 138 meV/atom for Co, Ru, and Os, and -28, -36, -30, and -72 meV/atom for Ni, Rh, Pd, and Ir. Moreover, the bulk energy

difference between two phases is proportional to the measured cohesive energy⁶⁹ of the favorable crystal phase at ambient conditions. This is understandable, since for a given phase the cohesive energy manifests the binding strength between metal atoms. The larger the cohesive energy, the stronger the binding strength between metal atoms, and so for the energy difference between the two crystal phases.

For lattice constants of the TMs in Group I, the optimized a and c for the hcp phase with a lower bulk energy are all in good agreement with well-documented experiments, and the absolute differences are less than 1.1%.^{70–72} Fcc Co, Ru, and Os have been synthesized successfully recently.^{25,72–76} Meanwhile, calculated lattice constants of a for these TMs of the fcc phase also agree well with experimental measurements, and the absolute differences between them are less than 1.3%. For the TMs in Group II, the calculated lattice constants of a for the fcc phase with a lower bulk energy are in good agreement with experiment with differences of less than 1.4%.^{69,77,78} Compared to Group I, hcp phase synthesis for this group metal is difficult, and so far only hcp Ni, Rh, and Pd have been partially reported.^{79–82} The absolute differences between calculations and experimental measurements could be as large as $\sim 5\%$, possibly due to the poor crystalline state, size effect, and/or presence of ligand, etc.⁸³

Surface Energy and Wulff Morphology. Numerous surfaces for both phases, 13 for fcc and 12 for hcp, were considered in the present work, and the calculated surface energies for the TMs considered are given in Table 2 and Table 3, respectively. Based on the calculated individual surface energies, equilibrium morphologies of the fcc and hcp phases via Wulff construction are derived. Figure 2 and Figure

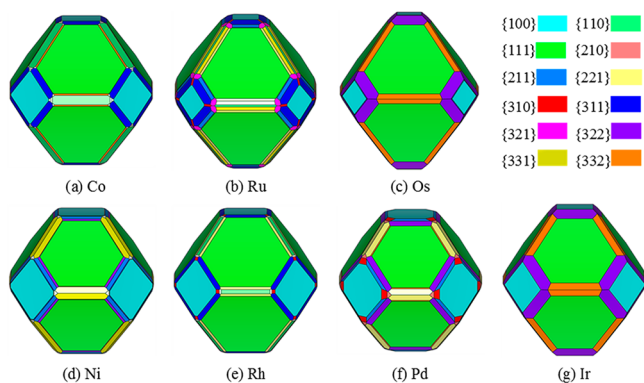


Figure 2. Optimized Wulff morphologies of late transition metals with the fcc crystal structure.

3 present the obtained thermodynamic equilibrium morphologies of the fcc and hcp phases, and the corresponding surface ratios are also given in Table 2 and Table 3, plotted in Figure 4 for better visualization.

For cobalt in Group I, we note that the $\{111\}$ facets have the lowest surface energy of $129 \text{ meV}/\text{\AA}^2$ among all fcc Co surfaces

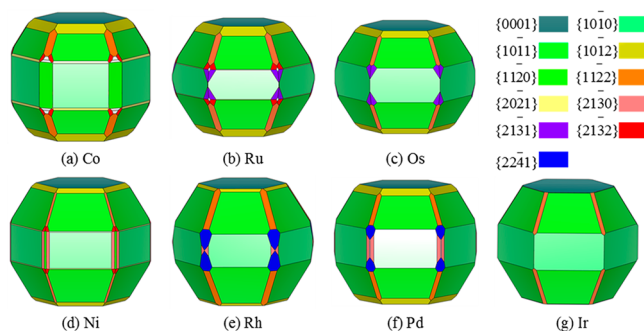


Figure 3. Optimized Wulff morphologies of late transition metals with the hcp crystal structure.

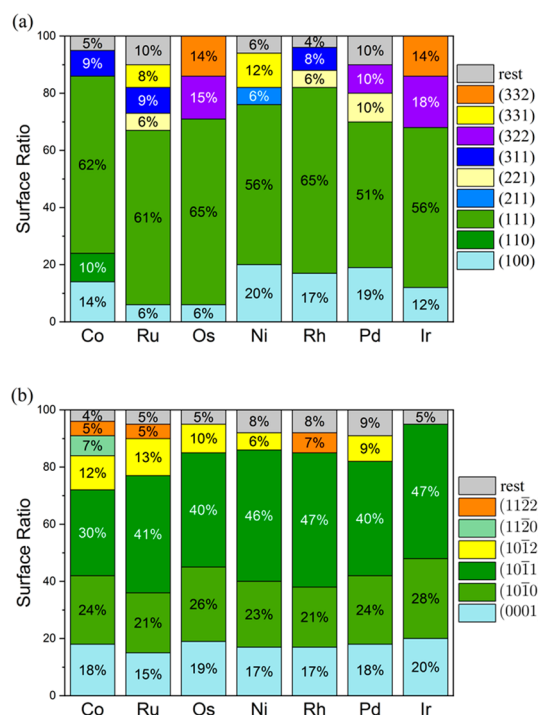


Figure 4. Surface ratio distributions in optimized Wulff morphologies of transition metals with (a) fcc and (b) hcp crystal structures. Those facets with surface ratio less than 5% are included in the “rest”.

considered, and the corresponding surface ratio is as high as 62%. The $\{110\}$, $\{100\}$, and $\{311\}$ facets have a relatively higher surface energy of 150 , 153 , and $156 \text{ meV}/\text{\AA}^2$, respectively, and the corresponding surface ratios are 10%, 14%, and 9%, respectively. The resulting overall surface energy is $136 \text{ meV}/\text{\AA}^2$. For hcp Co, the close-packed $\{0001\}$ facets have a surface energy of $131 \text{ meV}/\text{\AA}^2$ and only cover 18% of the surface area. The $\{10\bar{1}0\}$, $\{10\bar{1}1\}$, and $\{10\bar{1}2\}$ facets have surface energies of 141 , 149 , and $156 \text{ meV}/\text{\AA}^2$ and cover considerably 24%, 30%, and 12% of the surface area, respectively. In contrast, $\{11\bar{2}0\}$, $\{11\bar{2}2\}$, and $\{20\bar{2}1\}$ all together take ca. 15% of the surface area in hcp Co. The overall surface energy of hcp Co is $146 \text{ meV}/\text{\AA}^2$, $10 \text{ meV}/\text{\AA}^2$ higher than that of fcc Co.

The fcc Ru has a different morphology as compared with the fcc Co. First, new $\{221\}$ and $\{331\}$ facets with a surface energy of 165 and $169 \text{ meV}/\text{\AA}^2$ appear with a surface ratio of 6% and 8%, respectively. Along with this, the surface ratios of $\{100\}$ and $\{110\}$ facets decrease by 8%. For the $\{111\}$ and $\{311\}$ facets, their surface energies are 148 and $183 \text{ meV}/\text{\AA}^2$, and the corresponding surface ratios are 61% and 9%, respectively. The overall surface energy of fcc Ru becomes $159 \text{ meV}/\text{\AA}^2$. For hcp Ru, the surface ratio of $\{10\bar{1}1\}$ facets with a surface energy of $180 \text{ meV}/\text{\AA}^2$ increases significantly up to 41%. This is achieved mainly at the expense of the $\{0001\}$, $\{10\bar{1}0\}$, and $\{11\bar{2}0\}$ facets with surface energies of 163 , 181 , and $209 \text{ meV}/\text{\AA}^2$, respectively. The calculated overall surface energy of hcp Ru is $179 \text{ meV}/\text{\AA}^2$, $20 \text{ meV}/\text{\AA}^2$ higher than that of fcc Ru.

Changing from 3d Co, 4d Ru to 5d Os, the $\{100\}$ ratio decreases gradually, and the $\{110\}$ facets are even diminished. High-index facets, for example, the $\{322\}$ and $\{332\}$ facets of fcc Os, increase and together take 29% of the surface area with a surface energy of 190 and $183 \text{ meV}/\text{\AA}^2$, respectively. The $\{111\}$ facets with a surface energy of $168 \text{ meV}/\text{\AA}^2$ occupy

dominantly 65% of the surface area. The overall surface energy of fcc Os is 179 meV/Å². The hcp Os has a similar Wulff morphology as hcp Ru. The ratio of {1012} with a surface energy of 225 meV/Å² decreases to 10%, whereas the surface ratios of the {0001} and {1010} facets increase slightly to 19% and 26% with a surface energy of 182 and 213 meV/Å², respectively. {1011} facets with a surface energy of 216 meV/Å² remain the most abundant facets with the surface ratio of 40%. The resulting overall surface energy of hcp Os is 213 meV/Å², 34 meV/Å² higher than that of fcc Os.

We then turn to the TMs of Ni, Rh, Pd, and Ir in Group II preferring the fcc phase at ambient conditions. For fcc Ni, the {111} surface energy is slightly lower with a value of 119 meV/Å², as compared with Co, and the corresponding ratio decreases slightly to 56%. The {100} ratio is as high as 20%, which is actually the highest one among the TMs considered. There are considerable {331} facets exposed with a ratio of 12%, which is only about 8% for Ru but zero for the remaining TMs considered. The resulting overall surface energy is 125 meV/Å². As compared with hcp Co, the Ni {1011} ratio with a surface energy of 124 meV/Å² increases to 46% at the cost of {1012}, {1120}, and {1122} facets. The {0001} and {1010} facets have surface energies of 115 and 121 meV/Å² and occupy 17% and 23% of the surface area, respectively. The resulting overall surface energy of the hcp Ni is 122 meV/Å², 3 meV/Å² lower than that of the fcc Ni.

For fcc Rh, the {111} facets have a surface energy of 125 meV/Å² and cover 65% of the surface area, which is indeed the highest one among the TMs considered. The next populated facets are {100}, and the corresponding surface ratio and surface energy are 17% and 145 meV/Å². The remaining facets exposed are {311}, {221}, and {110} with ratios of 8%, 6%, and 4%, respectively. The calculated overall surface energy is 134 meV/Å². For hcp Rh, the {1011} facets have a surface energy of 130 meV/Å², and they are the most populated facets with a ratio of 47%. The next three populated facets are {1010}, {0001}, and {1122} with ratios of 21%, 17%, and 7%, respectively, and the corresponding surface energies are 129, 122, and 141 meV/Å². The calculated overall surface energy of the hcp Rh is 132 meV/Å², only 2 meV/Å² lower than that of the fcc Rh.

Pd is just on the right side of Rh in the periodic table. Compared to fcc Rh, the ratio of the {111} facets with a surface energy of 83.3 meV/Å² decreases to 51%. The surface ratios of {100}, {221}, and {322} facets remain considerable with ratios of 19%, 10%, and 10%, and the corresponding surface energies are 94.1, 93.1, and 90.8 meV/Å². The remaining 10% of the surface area is populated by, for instance, {211}, {310}, {332}, and {210}. The resulting overall surface energy is 87.4 meV/Å², which is the lowest one among all fcc TMs considered. For hcp Pd, the {1011} facets have a surface energy of 87.2 meV/Å² and remain the most populated facets with a surface ratio of 40%. The {1010}, {0001}, and {1012} facets cover 24%, 18%, and 9% of the surface area, and the corresponding surface energies are 84.6, 77.9, and 93.0 meV/Å². The calculated overall surface energy of the hcp Pd is 85.2 meV/Å², still 2.2 meV/Å² lower than that of the fcc Pd.

The morphology of fcc Ir is close to that of fcc Os, and only {111}, {322}, {332}, and {100} facets are exposed with ratios of 56%, 18%, 14%, and 12%, respectively. The corresponding surface energies are 142, 157, 154, and 175 meV/Å². The resulting overall surface energy is 150 meV/Å². For hcp Ir, the exposed areas are nearly completely occupied by {1011},

{1010}, and {0001} facets with ratios of 47%, 28%, and 20% (95% in total). The calculated surface energies are 146, 142, and 132 meV/Å², respectively. The resulting overall surface energy is 141 meV/Å². It is 9 meV/Å² lower than that of fcc Ir, and although modest, it still relatively larger than the difference of Pd, Rh, and Ni discussed above.

From the above results, it is clear that the equilibrium morphologies of the fcc TMs are in general truncated octahedron-like shape, and the {111} and {100} facets are preferentially exposed and cover the surface area of 67% at least. The equilibrium morphologies of the hcp TMs are all dihedral-like in shape, and the {0001}, {1010}, and {1011} facets dominate the surface area of 72% at least. As shown in Figure 4, there remain some changes in the exposed facets and ratios dependent on the composition, which are modest anyhow.

Trend Variation of the Overall Surface Energy and Compensation Effect. To see the trend variation, we plot the calculated overall surface energies for all TMs considered in both the hcp and fcc phases with respect to the experimental cohesive energy in Figure 5a. With gradual increase of the

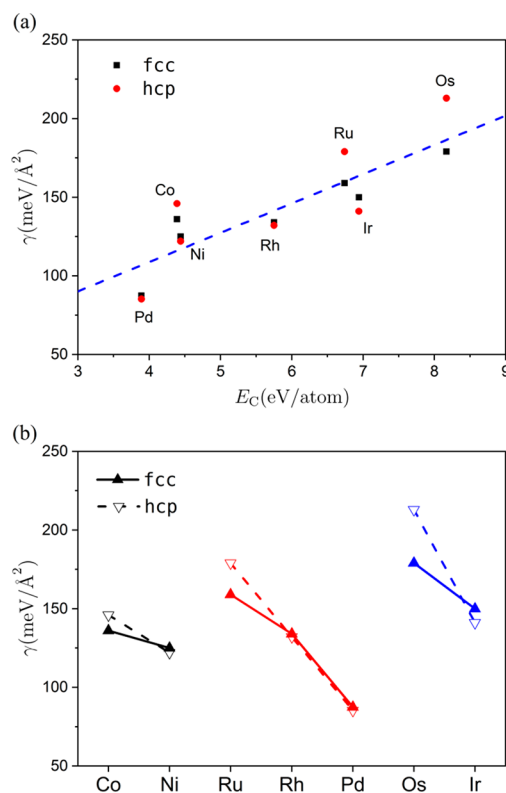


Figure 5. Overall surface energies with respect to the cohesive energy of transition metals (a) and 3d, 4d to 5d transition metals (b) considered.

cohesive energy of Pd, Co, Ni, Rh, Ru, Ir, and Os from 3.89 to 8.17 eV/atom,⁶⁹ the corresponding overall surface energies increase proportionally from 85.2 to 213 meV/Å². A good linear correlation is identified: the higher the cohesive energy, the larger the overall surface energy, which is reasonable. The present results are in good agreement with earlier experiments, where the surface tension for many liquid and solid metals was found to depend linearly on the corresponding vaporization or sublimation energy,⁸⁴ which correlates directly with the cohesive energy.

We also plot the overall surface energies with respect to the occupation of the valence electrons for the TMs in Figure 5b. Independent of the 3d, 4d, and 5d TMs, the calculated surface energies for both the hcp and fcc phases decrease systematically with an increase of the occupation of d valence electrons. For TMs with more valence electrons occupied and lower-lying d-band center with respect to the Fermi level,⁸⁵ the tendency for the orbital hybridization between the TM atoms is weakened, a fact that would lower the energy cost to break the metal–metal bond resulting in a lower surface energy. From Figure 5b, it is interesting to note that for the increase of every valence electron, the decrease in surface energies for 3d hcp and fcc TMs are 24 and 11 meV/Å², respectively. For 4d hcp and fcc TMs, the extent of decreases in the surface energies increases considerably to 47 and 36 meV/Å² on average, and for 5d hcp and fcc TMs increases further up to 72 and 29 meV/Å², respectively. The trend behavior was also in line with previous results, where the surface energies of the TMs show a parabolic dependence on the d occupation and specifically decrease monotonically for the TMs in the right side of the periodic table.⁸⁶

It can be found from Figure 5a that for the TMs in Group I, the fcc surface energies are lower than those of the hcp phase, and the corresponding surface energy differences between fcc and hcp ($\Delta\gamma(\text{fcc} - \text{hcp})$) are -10 , -20 , and -34 meV/Å² for Co, Ru, and Os, respectively. However, for the TMs in Group II, the fcc surface energies are higher than those of hcp, and the corresponding $\Delta\gamma$ are 3, 2, 2.2, and 9 meV/Å² for Ni, Rh, Pd, and Ir, respectively. The relative order of the surface energy between fcc and hcp is reversed, although the corresponding differences are much smaller. The distinct behavior for the TMs between Group I and II is clearly seen in Figure 6a. Moreover, $\Delta\gamma$ is proportional to E_C : the larger the cohesive energy, the larger the absolute value of the difference, irrespective of the TMs in Group I or II. This is comprehensible since the TMs having a larger cohesive energy implies a stronger metal–metal bond, leading a relative larger surface energy and subsequently the difference between the two phases.

We note that in Figure 1, the bulk energy difference between fcc and hcp ΔE_B is also proportional to the cohesive energy. However, the order between the fcc and hcp phase is completely different with respect to the above surface energy difference as shown in Figure 6a. For the TMs in Group I, fcc bulk energies are higher than those of hcp, but the corresponding surface energies are lower. For the TMs in Group II, the fcc bulk energies are lower than those of hcp, and the corresponding surface energies are higher. This indicates that the higher the bulk energy of a crystal phase, the lower the corresponding surface energy, and the sign of $\Delta\gamma$ is opposite to that of ΔE_B . To better see this, $\Delta\gamma$ is plotted with respect to ΔE_B in Figure 6b. As expected, a perfect linear relationship between $\Delta\gamma$ and ΔE_B is found, and the corresponding slope is negative with a value of -0.18 .

To rationalize the result, we note that for the TMs in Group I at ambient conditions, the hcp phase is an energetically more favorable phase with a lower total energy than that of the fcc phase, and a lower total energy indicates a stronger metal–metal bond. As a result, a higher energy cost would be required to create new surfaces by truncating the corresponding metal–metal bond, and the resulting hcp surface energy is higher. Similarly, for the TMs in Group II metals at ambient conditions, the fcc phase is a favorable phase and has a

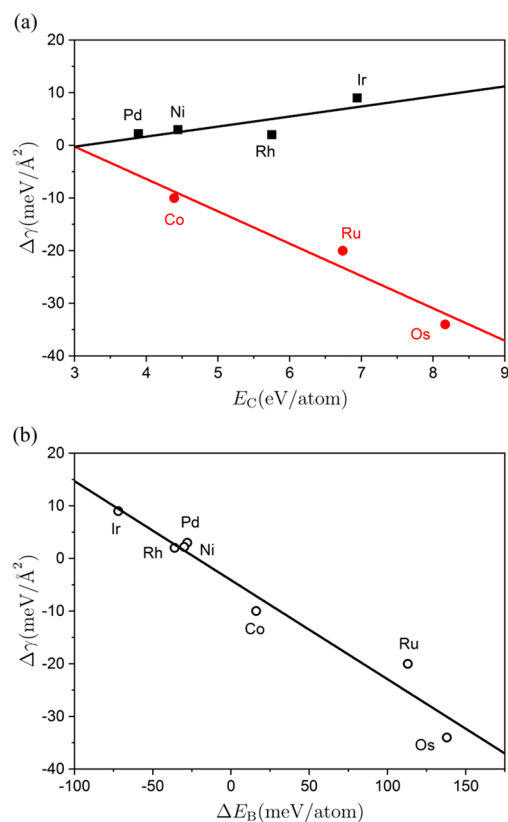


Figure 6. Calculated overall surface difference $\Delta\gamma$ between the fcc and hcp phase with respect to the cohesive energy E_C (a) and the bulk energy difference between the fcc and hcp phase ΔE_B (b).

lower total energy, and the corresponding surface energy would be higher. In other words, for a given TM, the favorable bulk phase with a lower total energy would have a higher surface energy as compensation. The compensation effect rationalizes the opposite sign of $\Delta\gamma$ and ΔE_B as well as their negative slope. Actually, the slope of the measured surface tension with respect to the vaporization energy above-mentioned is about $\sim 1/6$,⁸⁴ which is very close to our absolute slope calculated above.

DISCUSSION

The compensation effect between the crystal bulk energy and the corresponding surface energy found above would have a great impact on the relative stability of different close-packed phases for the TMs at a small size region particularly in the range of nanometers, where the surface energy plays a significant role in the overall energy. As a matter of fact, the overall energy of nanoparticle per atom, E_{NP} , taking the surface energy contribution into account from the Gibbs–Thomson equation by assuming the particle in a spherical shape with a curvature of radius R ,^{87–89} could be written as

$$E_{NP} = E_B + \frac{3\Omega\gamma}{R} \quad (4)$$

where Ω is the atomic volume. Concerning the overall energy E_{NP} of a given nanoparticle, the contribution of E_B is constant, but the surface energy term increases rapidly with the decrease of R . For nanoparticles with higher bulk energy, the corresponding surface energy is lower due to the compensation effect. For a given nanoparticle, the corresponding E_{NP} might

become lower than that with a lower bulk energy but a higher surface energy. As a result, by gradual decrease of the particle size to a critical value, the corresponding nanoparticles would transit from a favorable bulk phase to an unfavorable one but with an overall lower total energy, in the case of possible kinetics.

For the TMs of Co, Ru, and Os in Group I preferring the hcp bulk at ambient conditions, the above analysis means that the corresponding nanoparticles might transit to the fcc structure at certain small sizes. However, for the TMs of Ni, Rh, Pd, and Ir in Group II preferring the fcc bulk at ambient conditions, the corresponding particles might transit to the hcp structure. Since the surface energy differences between the fcc and hcp phases for the TMs in Group I are larger than those in Group II (Figure 6b), the driving force for the phase transition is stronger and would happen easily.

The above discussions are in good agreement with available experiments. For the three TMs of Co, Ru, and Os in Group I, fcc phases have all been found and/or synthesized experimentally. Among other things, fcc Co was one of the most reported ones.^{90–97} When Co particles' sizes were larger than 40 nm, hcp Co was the predominant phase with a very small amount of fcc Co, and more fcc Co could be found when the particle size was less than 20 nm.⁷³ By using Ru precursor containing an optimum ligand and/or another TM as a template, fcc Ru nanoparticles were also synthesized.^{25,30,31,75} By adopting similar methods, fcc Os NPs with a size of 1.2 nm were synthesized very recently.⁷² In contrast, for the TMs in Group II, hcp phases were difficult to form, and so far only few have been reported, in line with the above analysis. Hcp Ni nanoparticles were observed by decreasing the particle size down to 4 nm,⁹⁸ and hcp Rh particles were synthesized by solvothermal reaction or electron-beam-induced decomposition of Rh monolayers.⁸¹

As already indicated above, different crystal phases might be prepared with the help of the optimum ligands by tuning the corresponding surface energies of specific phases and facets.⁹⁹ By utilizing the specific template with strong interfacial interaction, a novel crystal phase, such as fcc Ru shell over fcc Pt core, could be achieved as well.^{24,100–102} These together with tuning the particle size and strong metal support interaction provide effective ways to control the crystal phase of nanoparticles, which might be useful for designing better catalysts.

CONCLUSION

Based on density functional theory calculations, numerous surfaces of Co, Ru, Os, Ni, Rh, Pd, and Ir in both the fcc and hcp phases are investigated. From the calculated surface energies, equilibrium morphologies are constructed. Irrespective of the transition metals considered, the fcc phase is composed mainly of {111} and {100} facets, and the hcp phase is composed mainly of {10 $\bar{1}$ 0}, {10 $\bar{1}$ 1}, and {0001} facets. Hcp Co, Ru, and Os with a lower bulk energy have a higher surface energy than the fcc ones, whereas hcp Ni, Rh, Pd, and Ir with a higher bulk energy have a lower surface energy than the fcc ones. A negative linear dependence of the surface energy difference between the fcc and hcp phase on the corresponding bulk energy difference is revealed. The established compensation effect between the bulk energy of a crystal phase and the overall surface energy provides a driving force for the sized-induced phase transition of the support nanoparticles, and the insights revealed might be used to design better catalysts.

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Notes

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