

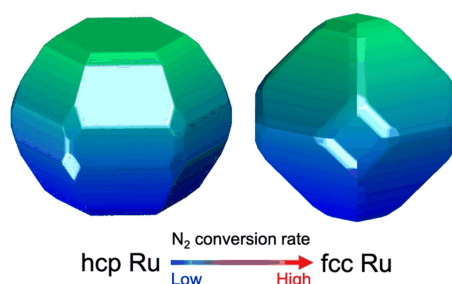
## ARTICLE

Crystallographic and Morphological Sensitivity of N<sub>2</sub> Activation over RutheniumHao Lin<sup>a, d†</sup>, Jin-xun Liu<sup>b†</sup>, Hong-jun Fan<sup>a\*</sup>, Wei-xue Li<sup>b, c\*</sup>*a. State Key Laboratory of Molecular Reaction Dynamics, Dalian Institute of Chemical Physics, Chinese Academy of Science, Dalian 116023, China**b. Department of Chemical Physics, School of Chemistry and Materials Science, University of Science and Technology of China, Hefei 230026, China**c. Hefei National Laboratory for Physical Science at the Microscale, iCHEM, University of Science and Technology of China, Hefei 230026, China**d. University of Chinese Academy of Sciences, Beijing 100049, China*

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Ruthenium (Ru) serves as a promising catalyst for ammonia synthesis via the Haber-Bosch process, identification of the structure sensitivity to improve the activity of Ru is important but not fully explored yet. We present here density functional theory calculations combined with microkinetic simulations on nitrogen molecule activation, a crucial step in ammonia synthesis, over a variety of hexagonal close-packed (hcp) and face-center cubic (fcc) Ru facets. Hcp {2130} facet exhibits the highest activity toward N<sub>2</sub> dissociation in hcp Ru, followed by the monatomic step sites. The other hcp Ru facets have N<sub>2</sub> dissociation rates at least three orders lower. Fcc {211} facet shows the best performance for N<sub>2</sub> activation in fcc Ru, followed by {311}, which indicates stepped surfaces make great contributions to the overall reactivity. Although hcp Ru {2130} facet and monatomic step sites have lower or comparable activation barriers compared with fcc Ru {211} facet, fcc Ru is proposed to be more active than hcp Ru for N<sub>2</sub> conversion due to the exposure of the more favorable active sites over step surfaces in fcc Ru. This work provides new insights into the crystal structure sensitivity of N<sub>2</sub> activation for mechanistic understanding and rational design of ammonia synthesis over Ru catalysts.

**Key words:** Ammonia synthesis, N<sub>2</sub> activation, Density functional theory, Ru, Crystallographic and morphological sensitivity



## I. INTRODUCTION

Ammonia synthesis via Haber-Bosch process has played a crucial role in the development of the chemical industry during the 20th century [1, 2]. Industrially, the Haber-Bosch process is mainly operated at elevated temperature and pressure [3, 4], typically catalyzed by Fe [5–10] and Ru [11–16] catalysts. Due to the broad range of applications and the vital importance, the synthesis of ammonia is probably the most extensively studied reaction in heterogeneous catalysis

[17, 18]. A large number of experimental and theoretical studies have been devoted to elucidating the reaction mechanism and identifying the active sites of ammonia synthesis reaction [19–23]. It has been well established that dissociative chemisorption of N<sub>2</sub> is particularly structure-sensitive and N<sub>2</sub> dissociation is often considered as the rate-determining step over Fe and Ru catalysts [16, 24–28]. Deeper insight into the structure sensitivity and active site distribution of N<sub>2</sub> activation is a significant way to improve particularly the mass-specific activity of Ru with economic efficiency.

The structure sensitive N<sub>2</sub> activation and ammonia synthesis were studied extensively before, mainly on hexagonal close-pack (hcp) Ru [29]. Surface experiments combined with the density functional theory (DFT) calculations showed that ammonia synthesis over Ru should also be a very structure-sensitive reac-

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tion [12, 13], even more obviously than on Fe. Dahl *et al.* showed that the dissociative chemisorption of nitrogen over Ru (0001) surface are dominated by the so-called  $B_5$  sites located at the surface steps [30].  $N_2$  adsorption/desorption rates at the terraces are several orders of magnitude lower than that at the step  $B_5$  sites [13]. Therefore,  $B_5$  sites were proposed active for  $N_2$  dissociation on Ru nanoparticles, which has a maximum  $NH_3$  synthesis activity at 2 nm [18]. Raróg-Pilecka *et al.* showed that the turnover frequency of  $NH_3$  synthesis increased as the particle size increased from 0.7 nm to 4 nm. Extrapolation to lower sizes indicates that Ru crystallites smaller than 0.7–0.8 nm might be totally inactive [28], due to the lack of  $B_5$  sites which is not available at small size otherwise. However, Kim *et al.* demonstrated that the sites presented on a double-stepped Ru (109) surface are relatively more active than the stepped Ru (0001) surface [31]. Shetty *et al.* studied Ru (11 $\bar{2}$ 1) surface can be active for  $N_2$  dissociation [32]. Recently,  $N_2$  activation was studied over a variety of planar Ru (0001), quasi-planar (10 $\bar{1}$ 1) step and edge sites by DFT calculations, and in addition to  $B_5$  sites, several competitive edge sites were found and could contribute to the overall reactivity [33]. Despite extensive investigations so far, only few representative surfaces together with corresponding step/edge sites are considered. For supported hcp Ru nanoparticles, the exposed sites are highly heterogeneous and their structure sensitivity as well as contributions to the overall activity for  $N_2$  activation remains open.

The impact of crystal structures on chemical reactions, in addition to morphology, has attracted much attention and been widely investigated in recent years [34–49]. For example, experiments found that hcp cobalt (Co) exhibits higher activity than face-center cubic (fcc) Co for Fischer-Tropsch synthesis (FTS) process [50–54]. DFT calculations revealed that hcp Co is significantly more active than fcc Co for CO and  $N_2$  activation, due to the sites available not only with lower barrier but also with higher abundance over hcp Co [55, 56]. On the other hand, fcc Ru was predicted to have a higher mass-specific activity for CO dissociation than hcp Ru for exposing the abundant sites though corresponding barriers were not the lowest one. Theoretical prediction was verified by subsequent experiment, where the synthesized fcc Ru shows extraordinary higher mass-specific activity than hcp Ru in FTS [46]. For  $N_2$  activation on fcc Ru, fcc Ru (111) and (001) surfaces were found to be more active than hcp Ru (0001) surface [57]. Whether and why the overall activity for  $N_2$  activation on fcc Ru is higher than hcp Ru was not studied yet.

To address the above questions,  $N_2$  activation on hcp Ru and fcc Ru was thoroughly investigated by DFT study in this work. Structure sensitivity were explored in depth by considering a number of facets in both hcp Ru and fcc Ru, and exposed facets and corresponding morphologies were determined by Wulff construction

based on the calculated surface energies.  $N_2$  activation was studied over all the exposed facets in the hcp Ru and fcc Ru Wulff shapes, and corresponding dissociation rate and conversion rate taking into account of the site distribution were calculated. The crystal structure sensitivity of hcp Ru and fcc Ru along with rational design for more effective Ru-based catalysts for  $N_2$  dissociation and ammonia synthesis were discussed finally.

## II. COMPUTATIONAL DETAILS

All the DFT calculations were performed by using the Vienna *ab initio* simulation package (VASP) [58, 59]. Projector augmented wave potentials [60] and the generalized gradient approximation with the Perdew-Burke-Ernzerhof exchange-correlation functionals [61] were adopted. The plane wave cutoff energy was specified by 400 eV and the convergence threshold for geometry optimizations was set to  $10^{-4}$  eV. When all the forces on the atoms are less than 0.01 eV/Å, the geometry optimizations are considered to be converged. Monkhorst-Pack [62] mesh  $k$ -points samplings of (12×12×1) and (10×10×1) were used for the bulk hcp Ru and fcc Ru calculations, respectively. The optimized lattice constants of hcp Ru are  $a=2.728$  Å and  $c/a=1.575$ , which are in good agreement with the experimental values of  $a=2.70$  Å and  $c/a=1.582$  [63]. The calculated lattice constant fcc Ru was 3.818 Å, in line with the experimental measurement [64].

The p(2×2) slab models of hcp Ru and fcc Ru surfaces usually have metal layers of 6–9 Å thickness. The stepped hcp Ru (0001) surface was modeled by a p(3×4) slab with removing two rows Ru atoms on the surface. Neighboring slabs are separated by a vacuum of 15 Å, to avoid the interactions between them. We took the fcc Ru (111) surface as an example to describe the computational details. The Ru (111) surface was modeled with a four-layers slab, the bottom two layers were constrained at their bulk positions, and the top two Ru layers and adsorbed molecules were allowed to relax. All the other hcp Ru and fcc Ru surfaces were simulated by slabs resemble to four (111) layers thickness and relaxation constraints with the  $k$ -point density keeping at  $\sim 0.03/\text{Å}$  for all the slab calculations.

For a given surface, the adsorption energy is calculated as:

$$E_{\text{ads}} = E_{\text{ads/slab}} - E_{\text{slab}} - E_{\text{gas}} \quad (1)$$

where,  $E_{\text{ads/slab}}$ ,  $E_{\text{slab}}$  and  $E_{\text{gas}}$  are the total energies of Ru surface with an adsorbate, clean Ru surface, and corresponding gaseous molecule and radical, respectively.

The force reversed method [65] was used to determine the transition states (TS) within a force tolerance of 0.03 eV/Å. Some of the identified transition states were also characterized again by using the climbing-image nudged elastic band method (CI-NEB) [66] implemented in VASP to reaffirm the identified TS. Fre-

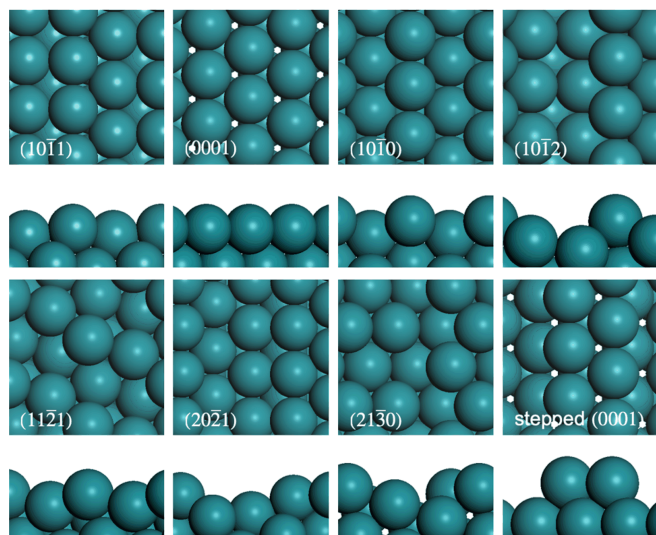


FIG. 1 Top and side view of bare hcp Ru surfaces.

quency analysis confirmed that all the located TS have only one imaginary frequency. We adopt the adsorbed N<sub>2</sub> molecules and the separated N atom in their most stable adsorption site as the initial and final states for N<sub>2</sub> activation, respectively.

### III. RESULTS AND DISCUSSION

#### A. Morphologies of hcp Ru and fcc Ru

The thermodynamic equilibrium shapes of hcp Ru and fcc Ru can be obtained by the Wulff construction based on the calculated surface energies [67]. The Wulff shapes and corresponding surface area proportions of the exposed surfaces in hcp Ru and fcc Ru were presented in our previous work [68], and FIGs. 1 and 2 show the top view and side view of all the clean surfaces considered in the present work. Obviously, the differences in stacking sequence and point group symmetries result in different morphologies between hcp Ru and fcc Ru [69].

The morphologies of hcp Ru and fcc Ru are dihedral-like and octahedron-like shapes, respectively. From our previous work, we have found that {0001} facets have the highest stability, followed by {1011}, {1010}, {2021}, {1012}, {1121}, and {2130} facets for hcp Ru with the surface energies of 160, 177, 181, 184, 188, 200 and 202 meV/Å<sup>2</sup>, respectively. The surface area of a specific facet is determined by not only the surface energy but also the orientations. {1011} facets group has the highest surface area proportion in hcp Ru Wulff shape with a value of 54%. Whereas {0001} (18%), {1010} (16%) and {1012} (6%) facets cover the remaining morphology of hcp Ru dominantly. High-index corrugated facets are less exposed in hcp Ru morphology due to their high surface energies. Specifically,

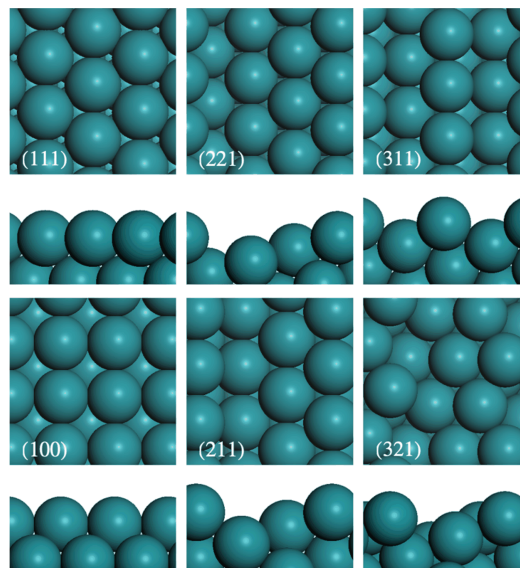


FIG. 2 Top and side view of bare fcc Ru surfaces.

{1121}, {2021}, and {2130} facets have the surface area proportion of 4%, 2% and 1%, respectively. Our predicted thermodynamic equilibrium morphology of hcp Ru is slightly different from that given by Nørskov *et al.* [18], which may originate from the calculated surface energies discrepancy caused by different potentials and exchange-correlation functionals.

When coming to fcc Ru, the exposed facets in fcc Ru Wulff shape are often {111}, {221}, {211}, {321}, {311} and {100} with the surface energies of 145, 163, 172, 174, 180, and 184 meV/Å<sup>2</sup>, respectively. In contrast to the flat {0001} surface in hcp Ru Wulff morphology, the close-packed {111} surface in fcc Ru has the lowest surface energy and takes as large as 63% of the total surface area in the fcc Ru Wulff shape, followed by {221} (14%), {311} (9%), {100} (6%), {211} (4%), and {321} (3%), respectively. N<sub>2</sub> activation was studied over all the exposed facets in hcp Ru and fcc Ru below to identify their crystallographic structure effect and structure-sensitivity relationship.

#### B. N<sub>2</sub> and N adsorption

First of all, we studied the chemisorption of N<sub>2</sub> molecule and N atom at various high-symmetry sites of each facet exposed in the Wulff shapes of hcp Ru and fcc Ru. The energetic and geometric information for N<sub>2</sub> molecules and N atoms adsorption over various hcp Ru and fcc Ru facets are listed in Table I. The corresponding most stable N atom adsorption configurations over hcp Ru and fcc Ru facets are shown in FIG. 3 and FIG. 4, respectively. N<sub>2</sub> molecule always prefers to bind perpendicularly to the topmost layered Ru atoms over all the hcp Ru and fcc Ru facets. The calculated N<sub>2</sub> ad-

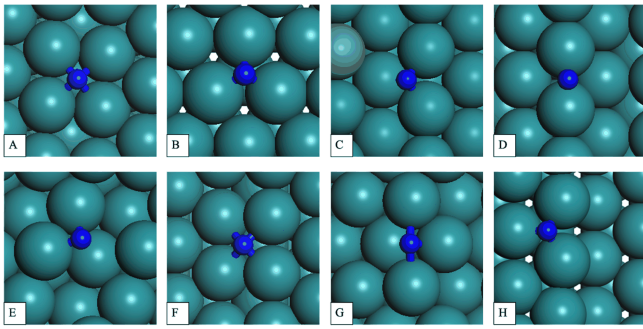


FIG. 3 Top view of N atom adsorbed on hcp Ru surfaces: (A)  $(10\bar{1}1)$ , (B)  $(0001)$  (C)  $(10\bar{1}0)$ , (D)  $(10\bar{1}2)$ , (E)  $(11\bar{2}1)$ , (F)  $(20\bar{2}1)$ , (G)  $(21\bar{3}0)$ , (H) stepped  $(0001)$ . The blue and cyan spheres represent the N and Ru atoms, respectively, and is used throughout this paper.

TABLE I Adsorption energy ( $E_{N_2}^{\text{ads}}$  and  $E_N^{\text{ads}}$ , eV) of  $N_2$  and N with respect to the corresponding gaseous molecule and radical, the selected adsorption geometric parameters ( $d_{N-N}$ , Å) for the most stable  $N_2$  and N atom adsorption site on hcp and fcc Ru surfaces.

Facet	$E_{N_2}^{\text{ads}}$	$d_{N-N}$	$E_N^{\text{ads}}$	Adsorption site
hcp $(10\bar{1}1)$	-0.72	1.135	-6.20	4-fold
$(0001)$	-0.61	1.135	-6.03	hcp-hollow
$(10\bar{1}0)$	-0.85	1.137	-5.82	3-fold
$(10\bar{1}2)$	-0.70	1.136	-5.92	bridge
$(11\bar{2}1)$	-0.79	1.137	-5.95	3-fold
$(20\bar{2}1)$	-0.85	1.136	-6.15	4-fold
$(21\bar{3}0)$	-0.92	1.139	-5.98	4-fold
Stepped $(0001)$	-0.86	1.138	-5.79	hcp-hollow
fcc $(111)$	-0.61	1.136	-6.30	hcp-hollow
$(221)$	-0.76	1.137	-5.96	bridge
$(311)$	-0.80	1.138	-6.08	edge-hcp
$(100)$	-0.71	1.136	-6.34	4-fold
$(211)$	-0.86	1.138	-6.36	edge-hcp
$(321)$	-0.85	1.137	-6.36	edge-hcp

sorption energies ( $E_{N_2}^{\text{ads}}$ ) vary from  $-0.61$  eV/ $(0001)$  to  $-0.92$  eV/ $(21\bar{3}0)$  for hcp Ru and from  $-0.61$  eV/ $(111)$  to  $-0.86$  eV/ $(211)$  for fcc Ru facets. Generally,  $N_2$  molecule adsorbs weaker on close-packed hcp Ru  $(0001)$  and fcc Ru  $(111)$  surface than those on the other corrugated facets containing more unsaturated surface Ru atoms. The overall variation of  $N_2$  adsorption energies among different facets are  $0.31$  eV for hcp Ru and  $0.25$  eV for fcc Ru, indicating less structure sensitivity.

Different from  $N_2$  adsorption, N atom prefers to coordinate with more surface Ru atoms (Table I, FIG. 3, and FIG. 4). N adsorption is structurally more sensitive as compared with  $N_2$  adsorption. N atom adsorption energies vary from  $-5.79$  eV to  $-6.20$  eV for hcp Ru and from  $-5.96$  eV to  $-6.36$  eV for fcc Ru. Specifically, N atom adsorbs strongly at the 4-fold sites

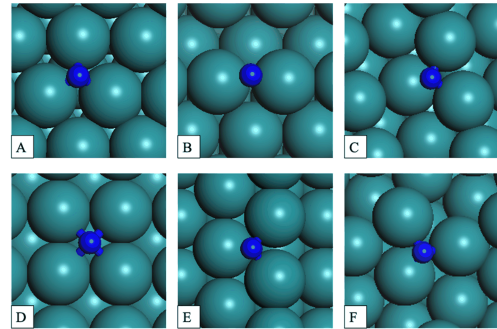


FIG. 4 Top view of N atom adsorbed on fcc Ru surfaces: (A)  $(111)$ , (B)  $(221)$ , (C)  $(311)$ , (D)  $(100)$ , (E)  $(211)$ , (F)  $(321)$ .

of  $(10\bar{1}1)$ ,  $(20\bar{2}1)$  and  $(21\bar{3}0)$  facets with the adsorption energies of  $-6.20$ ,  $-6.15$  and  $-5.98$  eV, respectively. Whilst N atom adsorbs at the 3-fold site which is less favorable over  $(0001)$  ( $-6.03$  eV),  $(11\bar{2}1)$  ( $-5.95$  eV),  $(10\bar{1}0)$  ( $-5.82$  eV) and stepped  $(0001)$  ( $-5.79$  eV) facets. However, N atom is more likely to adsorb at the bridge site on  $(10\bar{1}2)$  surface with an adsorption energy of  $-5.92$  eV. For fcc Ru surfaces, N atom adsorbs favorably at the edge-hcp site of  $(211)$ ,  $(321)$  and  $(311)$  facets with the adsorption energies of  $-6.36$ ,  $-6.36$  and  $-6.08$  eV, respectively. On  $(111)$  and  $(100)$  surface, N atom has nearly the same adsorption energies ( $-6.30$  eV *vs.*  $-6.34$  eV) at hcp-hollow and 4-fold sites, respectively. N atom adsorbs the weakest at the bridge site over the  $(221)$  facet with an adsorption energy of  $-5.96$  eV. In a word, N atom adsorbs stronger on most of the fcc Ru facets than on hcp Ru  $(10\bar{1}1)$  facet which binds N atom strongest among all the exposed facets in hcp Ru Wulff shape. The adsorption energy of N atom increases with the coordination number of N atom binding to the surface Ru atoms. N adsorption strength follows the sequence at the adsorption site of  $4\text{-fold} > 3\text{-fold} > \text{bridge}$  site. The large variation of  $N_2$  and N adsorption energies among different hcp Ru and fcc Ru facets will result in a great structure sensitivity of  $N_2$  activation.

### C. $N_2$ Dissociation

$N_2$  activation is systematically studied over all the exposed facets in the Wulff shapes of hcp Ru and fcc Ru. Activation barrier and the reaction enthalpy of  $N_2$  dissociation with respect to  $N_2$  at their most stable adsorption site are shown in Table II. The TS configurations are given in FIG. 5 and FIG. 6 for hcp Ru and fcc Ru, respectively.

$N_2$  dissociation reaction is highly exothermic and the reaction energies vary greatly among different hcp Ru and fcc Ru facets. Reaction energy of  $N_2$  activation is determined by both the  $N_2$  and N atom adsorption energies. The reaction energies for  $N_2$  activation vary from  $-0.41$  eV/ $(10\bar{1}0)$  to  $-1.29$  eV/ $(10\bar{1}1)$

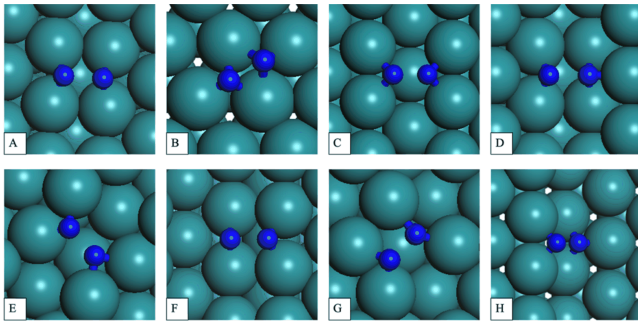


FIG. 5 Top view of N<sub>2</sub> dissociation TS structures on hcp Ru surfaces: (A) (10 $\bar{1}1$ ), (B) (0001), (C) (10 $\bar{1}0$ ), (D) (10 $\bar{1}2$ ), (E) (11 $\bar{2}1$ ), (F) (20 $\bar{2}1$ ), (G) (21 $\bar{3}0$ ), (H) stepped (0001).

TABLE II Calculated activation energies ( $E_a$ , in eV), reaction energies ( $\Delta H$ , in eV) with respect to N<sub>2</sub> at their most stable adsorption state, and the distance between the two N atoms ( $d_{N-N}$ , in Å) at TS for N<sub>2</sub> dissociation reaction on hcp Ru and fcc Ru surfaces.

Facet	$E_a$ /eV	$\Delta H$ /eV	$d_{N-N}/\text{Å}$
hcp (10 $\bar{1}1$ )	1.03	-1.29	1.861
(0001)	1.69	-1.07	1.726
(10 $\bar{1}0$ )	1.22	-0.41	1.700
(10 $\bar{1}2$ )	1.25	-0.77	1.898
(11 $\bar{2}1$ )	1.05	-0.73	1.818
(20 $\bar{2}1$ )	1.18	-1.07	1.890
(21 $\bar{3}0$ )	0.77	-0.67	1.857
Stepped (0001)	0.82	-0.35	1.823
fcc (111)	1.38	-1.60	1.694
(221)	1.05	-0.79	1.797
(311)	1.01	-0.99	1.895
(100)	0.97	-1.59	1.900
(211)	0.81	-1.48	1.849
(321)	1.19	-1.49	1.867

for hcp Ru facets, whereas from -0.79 eV/(221) to -1.60 eV/(111) for fcc Ru facets. The activation barriers for N<sub>2</sub> dissociation were calculated to be in the region of 0.77 eV/(21 $\bar{3}0$ )-1.69 eV/(0001) for all the hcp Ru facets including the stepped (0001) surface and 0.81 eV/(211)-1.38 eV/(111) for the fcc Ru facets. On the close-packed hcp Ru (0001) and fcc Ru (111) facets, the two N atoms are located at the fcc and hcp hollow site at the TS of N<sub>2</sub> dissociation, which is consistent with Crawford and Hu's findings [70]. Since two N atoms share two surface Ru metal atoms at the TS of N<sub>2</sub> dissociation, the large repulsive interaction between them gives rise to the highest N<sub>2</sub> dissociation barrier among all the hcp Ru and fcc Ru surfaces. Subsequently, the calculated N<sub>2</sub> activation barriers are 1.69 eV for hcp Ru (0001) and 1.38 eV for fcc Ru (111). Two N atoms sharing one Ru atom at TS decreases N<sub>2</sub> dissociation barrier to 1.22 eV on the hcp Ru (10 $\bar{1}0$ ) sur-

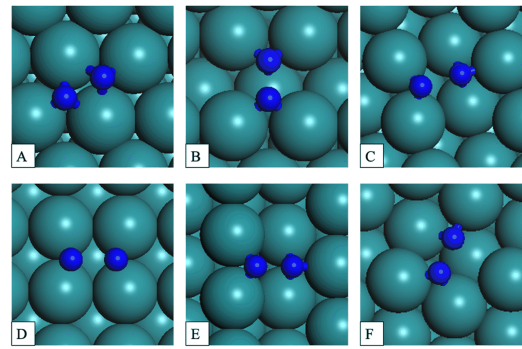


FIG. 6 Top view of N<sub>2</sub> dissociation TS structures on fcc Ru surfaces: (A) (111), (B) (221), (C) (311), (D) (100), (E) (211), (F) (321).

face. Whereas on the hcp Ru (10 $\bar{1}1$ ), (20 $\bar{2}1$ ), stepped (0001) and fcc Ru (100) facets, the two N atoms are located at the bridge sites in TS without sharing any Ru atoms, which results in the N<sub>2</sub> dissociation barrier lower by more than 0.04 eV. Whereas, on the other hcp and fcc Ru facets, one N atom sits at the 3-fold site and the other N atom moves to the bridge site in the TS without sharing Ru atoms, which will even lower the N<sub>2</sub> dissociation barrier. Specifically, the calculated N<sub>2</sub> dissociation barriers are 1.05, 0.77, 1.05, 1.01, 0.81 and 1.19 eV on hcp Ru (11 $\bar{2}1$ ) and (21 $\bar{3}0$ ), fcc Ru (221), (311), (211) and (321) facets, respectively. It is obvious that N<sub>2</sub> dissociation reaction is structure sensitive and hcp Ru (21 $\bar{3}0$ ) and fcc Ru (211) surfaces have the highest activity (the lowest barrier) for N<sub>2</sub> dissociation reaction in hcp Ru and fcc Ru, respectively.

#### D. Micro-kinetic model for N<sub>2</sub> dissociation

To compare N<sub>2</sub> dissociation activities of hcp Ru and fcc Ru quantitatively, we have performed micro-kinetic simulation. By using the calculated energetics, N<sub>2</sub> dissociation and conversion rates on each facet exposed in hcp Ru and fcc Ru Wulff shapes are computed. Here, we assume N<sub>2</sub> dissociation on Ru surfaces obeying Langmuir-Hinshelwood (L-H) mechanism. N<sub>2</sub> molecules first chemisorb on Ru surface, and then adsorb N<sub>2</sub> molecule, dissociate into two N atoms:



Assuming N<sub>2</sub> adsorption process is very fast compared to dissociation so that N<sub>2</sub> adsorption and desorption are in equilibrium. The equilibrium constant  $K$  for N<sub>2</sub> adsorption is the ratio of the forward rate constant  $k_1$  to the backward rate constant ( $k_{-1}$ ):

$$K = \frac{k_1}{k_{-1}} = \frac{\theta_{\text{N}_2}}{\theta_* P_{\text{N}_2}} = \frac{K^0}{P_0} \quad (4)$$

TABLE III Equilibrium constant ( $K$ , in  $\text{Pa}^{-1}$ ), reaction rate constant ( $k_2$ , in  $\text{s}^{-1}$ ), reaction rate ( $r$ , in molecule-site $^{-1}\cdot\text{s}^{-1}$ ), active site number of  $1\text{ m}^2$  Ru catalysts ( $N_{\text{act}}$ ) and conversion rate ( $C$ , in molecule $\cdot\text{s}^{-1}$ ) for  $\text{N}_2$  dissociation process on hcp and fcc Ru surfaces.

	Facet	$K$	$k_2$	$r$	$N_{\text{act}}$	$C$
hcp Ru	(10 $\bar{1}$ 1)	$2.5\times 10^{-10}$	$3.8\times 10^5$	$2.4\times 10^2$	$4.0\times 10^{18}$	$9.5\times 10^{20}$
	(0001)	$4.0\times 10^{-11}$	$6.8\times 10^0$	$6.8\times 10^{-4}$	$2.8\times 10^{18}$	$1.9\times 10^{15}$
	(10 $\bar{1}$ 0)	$2.1\times 10^{-9}$	$1.7\times 10^4$	$8.7\times 10^1$	$1.4\times 10^{18}$	$1.2\times 10^{20}$
	(10 $\bar{1}$ 2)	$1.8\times 10^{-10}$	$1.0\times 10^4$	$4.4\times 10^0$	$3.4\times 10^{17}$	$1.5\times 10^{18}$
	(11 $\bar{2}$ 1)	$7.9\times 10^{-10}$	$2.8\times 10^5$	$5.4\times 10^2$	$1.9\times 10^{17}$	$1.0\times 10^{20}$
	(20 $\bar{2}$ 1)	$2.1\times 10^{-9}$	$3.2\times 10^4$	$1.7\times 10^2$	$8.2\times 10^{16}$	$1.4\times 10^{19}$
	(21 $\bar{3}$ 0)	$6.8\times 10^{-9}$	$2.9\times 10^7$	$4.7\times 10^5$	$3.2\times 10^{16}$	$1.5\times 10^{22}$
	Stepped (0001)	$2.5\times 10^{-9}$	$1.3\times 10^7$	$7.7\times 10^4$		
fcc Ru	(111)	$4.0\times 10^{-11}$	$1.2\times 10^3$	$1.2\times 10^{-1}$	$1.0\times 10^{19}$	$1.2\times 10^{18}$
	(221)	$4.8\times 10^{-10}$	$2.8\times 10^5$	$3.3\times 10^2$	$6.4\times 10^{17}$	$2.1\times 10^{20}$
	(311)	$9.3\times 10^{-10}$	$5.4\times 10^5$	$1.2\times 10^3$	$7.4\times 10^{17}$	$9.2\times 10^{20}$
	(100)	$2.1\times 10^{-10}$	$1.0\times 10^6$	$5.4\times 10^2$	$8.2\times 10^{17}$	$4.4\times 10^{20}$
	(211)	$2.5\times 10^{-9}$	$1.5\times 10^7$	$9.1\times 10^4$	$2.2\times 10^{17}$	$2.0\times 10^{22}$
	(321)	$2.1\times 10^{-9}$	$2.7\times 10^4$	$1.4\times 10^2$	$1.1\times 10^{17}$	$1.6\times 10^{19}$

where  $\theta_{\text{N}_2}$  and  $\theta_*$  stand for the surface coverages of  $\text{N}_2$  molecules and free sites on the Ru surface, respectively.  $P_{\text{N}_2}$  and  $P_0$  are the partial pressure of  $\text{N}_2$  gas and the stand pressure, respectively.  $\text{N}_2$  dissociation (Eq.(3)) is irreversible and it is the rate-determining step for ammonia synthesis. Therefore, the surface coverages of  $\text{N}_2$  molecule and free active sites obey the sum rule:

$$\theta_{\text{N}_2} + \theta_* = 1 \quad (5)$$

Combining Eq.(4) and Eq.(5), we can obtain:

$$\theta_{\text{N}_2} = \frac{K P_{\text{N}_2}}{1 + K P_{\text{N}_2}} \quad (6)$$

$$\theta_* = \frac{1}{1 + K P_{\text{N}_2}} \quad (7)$$

Principally,  $K^0$  can be calculated as follows:

$$K^0 = e^{-\Delta G^0/k_{\text{B}}T} \quad (8)$$

Where  $\Delta G^0$  is the change of the stand Gibbs free energy for  $\text{N}_2$  adsorption:

$$\begin{aligned} \Delta G^0 &= E_{\text{N}_2/\text{slab}}(T, P_0) - E_{\text{slab}}(T, P_0) - \mu_{\text{N}_2}(T, P_0) \\ &\approx E_{\text{N}_2/\text{slab}}(0\text{ K}, P_0) - E_{\text{slab}}(0\text{ K}, P_0) - \\ &\quad [E_{\text{N}_2}(0\text{ K}, P_0) + \Delta\mu_{\text{N}_2}(T, P_0)] \\ &= E_{\text{N}_2}^{\text{ads}} - \Delta\mu_{\text{N}_2}(T, P_0) \end{aligned} \quad (9)$$

where  $E_{\text{N}_2}^{\text{ads}}$  is the adsorption energy of the  $\text{N}_2$  molecule.  $E_{\text{N}_2/\text{slab}}(0\text{ K}, P_0)$ ,  $E_{\text{slab}}(0\text{ K}, P_0)$  and  $E_{\text{N}_2}(0\text{ K}, P_0)$  are the total energies of  $\text{N}_2$  adsorption on the Ru surface system, clean slab surface and gaseous  $\text{N}_2$  molecule, respectively. While  $\mu_{\text{N}_2}(T, P_0)$  stands for the standard chemical potentials of  $\text{N}_2$  in the gas phase. In order to obtain  $\Delta\mu_{\text{N}_2}(T, P_0)$ , entropy and enthalpy changes

were taken from JANAF tables [71], as shown in the following equation

$$\Delta\mu_{\text{N}_2}(T, P_0) = H(T, P_0) - H(0\text{ K}, P_0) - TS(T, P_0) \quad (10)$$

Industrial ammonia synthesis conditions ( $T=700\text{ K}$ ,  $P=100\text{ bar}$ ,  $\text{N}_2$  to  $\text{H}_2$  ratio of 1:3, with 1% $\text{NH}_3$ ) were considered in our microkinetic simulations. Subsequently,  $\Delta\mu_{\text{N}_2}(700\text{ K}, 1\text{ bar})=-1.36\text{ eV}$  was applied in this work.

By using Eq.(3),  $\text{N}_2$  dissociation reaction rate can be written as

$$r = k_2\theta_{\text{N}_2}\theta_* = \frac{k_2 K P_{\text{N}_2}}{1 + K P_{\text{N}_2}} \quad (11)$$

The reaction rate constant  $k_2$  can be given by:

$$k_2 = A e^{-E_{\text{a}}/k_{\text{B}}T} \quad (12)$$

Here,  $A$  is the pre-factor,  $E_{\text{a}}$  denotes the  $\text{N}_2$  activation barrier and  $k_{\text{B}}$  is the Boltzmann constant. In order to estimate the reaction rate, we denoted the value of pre-factor  $A$  to be  $10^{13}\text{ s}^{-1}$ . Assuming all the active sites can be used for activating  $\text{N}_2$ , thus if we consider the total surface area of Ru nanoparticles to be  $1\text{ m}^2$ ,  $N_{\text{act}}$  represents the number of the active sites,  $\text{N}_2$  conversion rate  $C$  of a specified surface can be calculated as:

$$C = N_{\text{act}} \times r \quad (13)$$

Combining the above equations, we can derive the  $\text{N}_2$  reaction rate constants and conversion rates on all the hcp Ru and fcc Ru facets. The calculated equilibrium constant, reaction rate constant, reaction rate and conversion rate for all the facets considered are

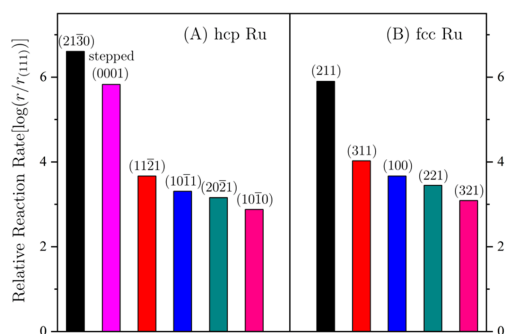


FIG. 7 Relative reaction rate for N<sub>2</sub> dissociation on hcp Ru and fcc Ru surfaces at  $T=700$  K,  $P=100$  bar. All rates  $r$  are normalized by that of fcc Ru (111) surface with units of molecule-site<sup>-1</sup>·s<sup>-1</sup>.

listed in Table III for hcp Ru and fcc Ru. N<sub>2</sub> dissociation rate is structure-sensitive and determined by N<sub>2</sub> adsorption energies and activation barriers. N<sub>2</sub> dissociation rate ( $r$ ) varies from  $6.8 \times 10^{-4}$  site<sup>-1</sup>·s<sup>-1</sup> to  $4.7 \times 10^5$  site<sup>-1</sup>·s<sup>-1</sup> and from  $1.2 \times 10^1$  site<sup>-1</sup>·s<sup>-1</sup> to  $9.1 \times 10^4$  site<sup>-1</sup>·s<sup>-1</sup> among all the facets exposed in hcp Ru and fcc Ru Wulff shapes, respectively. For hcp Ru, the {2130} facet has the highest reaction rate ( $4.7 \times 10^5$  site<sup>-1</sup>·s<sup>-1</sup>) which is at least three orders of magnitude higher than other facets. Whereas, the stepped hcp Ru {0001} surface has the second highest N<sub>2</sub> activation rate ( $7.7 \times 10^4$  site<sup>-1</sup>·s<sup>-1</sup>). N<sub>2</sub> dissociation rates for the remaining facets decrease following the sequence: {1121} ( $5.4 \times 10^2$  site<sup>-1</sup>·s<sup>-1</sup>), {1011} ( $2.4 \times 10^2$  site<sup>-1</sup>·s<sup>-1</sup>), {2021} ( $1.7 \times 10^2$  site<sup>-1</sup>·s<sup>-1</sup>), {1010} ( $8.7 \times 10^1$  site<sup>-1</sup>·s<sup>-1</sup>), {1012} ( $4.4$  site<sup>-1</sup>·s<sup>-1</sup>) and {0001} ( $6.8 \times 10^{-4}$  site<sup>-1</sup>·s<sup>-1</sup>). For fcc Ru, the stepped {211} facet has the largest reaction rate of  $9.1 \times 10^4$  site<sup>-1</sup>·s<sup>-1</sup>; {311}, {100} and {221} surfaces have very similar reaction rates ranging from  $1.2 \times 10^3$  site<sup>-1</sup>·s<sup>-1</sup> to  $3.3 \times 10^2$  site<sup>-1</sup>·s<sup>-1</sup>. However, {321} and {111} surfaces are less active for N<sub>2</sub> dissociation with the reaction rates of  $1.4 \times 10^2$  site<sup>-1</sup>·s<sup>-1</sup> and  $1.2 \times 10^{-1}$  site<sup>-1</sup>·s<sup>-1</sup>, respectively.

Taking into account the number of the active sites of a specific facet, we gave the conversion rate of each facet exposed in the hcp Ru and fcc Ru Wulff shapes except for the stepped hcp Ru {0001}. From Table III, we can see that the conversion rate follows the sequence by {2130} > {1011} > {1010} > {1121} > {2021} > {1012} > {0001} for hcp Ru varying from  $1.5 \times 10^{22}$  s<sup>-1</sup> to  $1.9 \times 10^{15}$  s<sup>-1</sup>, whereas {211} > {311} > {100} > {221} > {321} > {111} for fcc Ru varying from  $2.0 \times 10^{22}$  s<sup>-1</sup> to  $1.2 \times 10^{18}$  s<sup>-1</sup>. To see N<sub>2</sub> dissociation activity intuitively, the relative reaction rate of hcp Ru and fcc Ru facets referring to the reaction rate value of fcc {111} are also plotted in FIG. 7. For hcp Ru, although {2130} surface has a small surface area ratio (1%), the lowest activation barrier of N<sub>2</sub> dissociation results in the highest N<sub>2</sub> conversion rate of  $1.5 \times 10^{22}$  s<sup>-1</sup>, which is a major contribution to the total conversion rate of hcp Ru.

The conversion rate for {1011} surface, which has the largest surface area, becomes only  $9.5 \times 10^{20}$  s<sup>-1</sup>, nearly the same as that for fcc Ru {311} surface. Meanwhile, fcc Ru {211} surface has the highest N<sub>2</sub> conversion rate of  $2.0 \times 10^{22}$  s<sup>-1</sup>, which are more than two orders higher than that of all the other fcc Ru surfaces.

By summarizing all the contributions of each facets, the calculated total conversion rate of fcc Ru for N<sub>2</sub> activation becomes  $2.2 \times 10^{22}$  s<sup>-1</sup> vs.  $1.6 \times 10^{22}$  s<sup>-1</sup> to that of hcp Ru even considering the most active hcp Ru {2130} facet. Given that when hcp Ru particle size is decreasing, hcp Ru {2130} surface will not be able to expose owing to its high surface energy. Therefore, fcc Ru is apparently more active than hcp Ru for N<sub>2</sub> activation due to the exposure of abundant step and edge sites on {211} surface. Additionally, there are eight {111} surfaces exposed in the Wulff shape of fcc Ru, while the Wulff shape of hcp Ru is covered by two {0001} surfaces. The step sites can form at the edge of flat surfaces and more monatomic step sites exposed in fcc Ru can enhance N<sub>2</sub> dissociation activity further.

Based on our DFT calculation studies, we propose here possible ways to design highly active Ru-based catalyst for ammonia synthesis. Fcc Ru catalyst should be synthesized to enhance N<sub>2</sub> dissociation activity by increasing the exposure of more {211} facets and step sites. Even for hcp Ru, there is still much room for improving the activity of N<sub>2</sub> activation by the usage of the highly active monatomic stepped sites on or at the edge of hcp Ru {0001} surface. Our work agrees well with the previous studies by Nørskov *et al.* that the stepped site on hcp Ru {0001} surface is considered as the active site for the ammonia synthesis process [16, 26, 72, 73].

Our previous DFT calculations indicated that hcp Co has higher N<sub>2</sub> dissociation activity than fcc Co due to the denser active sites with high intrinsic activity in hcp Co Wulff shape [56]. In principle, Ru is more active than Co for N<sub>2</sub> activation due to the lower activation barriers for N<sub>2</sub> dissociation on Ru. The difference between Co and Ru is that fcc Ru exhibits better performance than hcp Ru for N<sub>2</sub> activation. This can be attributed to the fact that Ru has larger lattice constants than Co [74], which results in different transition state configurations over the facets of Ru compared to Co.

#### IV. CONCLUSION

DFT calculations were performed to study the structure sensitivity of N<sub>2</sub> activation on hcp Ru and fcc Ru. First-principles kinetic study indicates that {2130} facet has the highest activity for N<sub>2</sub> activation in hcp Ru, followed by the monatomic step sites. Whereas the stepped {211} facet achieves best performance for N<sub>2</sub> activation in fcc Ru. Fcc Ru is more active than hcp Ru for N<sub>2</sub> conversion, which can be understood by the exposure of more active sites over the stepped {211} facet

and monatomic step in fcc Ru. Our work provides a pragmatic way to improve the mass-specific activity of N<sub>2</sub> dissociation by using fcc Ru catalysts.

## V. ACKNOWLEDGMENTS

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